

### Course Objectives:

#### To enable the students to –

- Analyze the solution of differential equations of the first order and of the first degree by variables separable, Homogeneous and Non-Homogeneous methods.
- Evaluate a solution of differential equations of the first order and of a degree higher than the first by using methods of solvable for p, x and y.
- Compute all the solutions of second and higher order linear differential equations with constant coefficients, linear equations with variable coefficients.
- Solve simultaneous linear equations with constant coefficients and total differential equations
- Find the solution of First order partial differential equations for some standard types
- Apply Laplace transform to solve second order linear differential equation and simultaneous linear differential equations
- Compute all the solutions of Higher Order Linear Differential Equations with Constant Coefficients and non-Constant Coefficients

### Course Outcomes

After successful completion of this course, the student will be able to

1. Solve first order first degree linear differential equations.
2. Convert a non-exact homogeneous equation to exact differential equation by using an integrating factor.
3. Know the methods of finding solution of a differential equation of first order but not of first degree.
4. Solve higher-order linear differential equations for both homogeneous and non-homogeneous, with constant coefficients.
5. Understand and apply the appropriate methods for solving higher order differential equations.

### COURSE CONTENT

#### UNIT – 1: DIFFERENTIAL EQUATIONS OF FIRST ORDER AND FIRST DEGREE:

Linear Differential Equations – Bernoulli's Equations - Exact Differential Equations –  
Integrating factors - Equations reducible to Exact Equations by Integrating Factors -

- i) Inspection Method      ii)  $\frac{1}{Mx+Ny}$       iii)  $\frac{1}{Mx-Ny}$

**UNIT – 2:****DIFFERENTIAL EQUATIONS OF FIRST ORDER BUT NOT OF FIRST DEGREE**

Equations solvable for  $p$ , Equations solvable for  $y$ , Equations solvable for  $x$  – Clairaut's equation - Orthogonal Trajectories: Cartesian and Polar forms.

**UNIT – 3****HIGHER ORDER LINEAR DIFFERENTIAL EQUATIONS:**

Solutions of homogeneous linear differential equations of order  $n$  with constant coefficients -

Solutions of non-homogeneous linear differential equations with constant coefficients by means of polynomial operators

$$(i) Q(x) = e^{ax} \quad (ii) Q(x) = \sin ax \text{ (or) } \cos ax$$

**UNIT – 4****HIGHER ORDER LINEAR DIFFERENTIAL EQUATIONS (CONTINUED.)**

Solution to a non-homogeneous linear differential equation with constant coefficients

P.I. of  $(D)y = Q$  when  $Q = bx^k$

P.I. of  $(D)y = Q$  when  $Q = e^{ax}V$ , where  $V$  is a function of  $x$

P.I. of  $(D)y = Q$  when  $Q = xV$ , where  $V$  is a function of  $x$

**UNIT – 5:****HIGHER ORDER LINEAR DIFFERENTIAL EQUATIONS WITH NON-CONSTANT COEFFICIENTS:**

Linear differential Equations with non-constant coefficients; Cauchy-Euler Equation; Legendre Equation; Method of variation of parameters

**ACTIVITIES :**

Seminar/ Quiz/ Assignments/ Applications of Differential Equations to Real life Problem /Problem Solving Sessions.

**TEXT BOOK :**

Differential Equations and Their Applications by Zafar Ahsan, published by Prentice-Hall of India Pvt. Ltd, New Delhi-Second edition.

**REFERENCE BOOKS:**

1. Ordinary and Partial Differential Equations by Dr. M.D. Raisinghania, published by S. Chand & Company, New Delhi.
2. Differential Equations with applications and programs – S. Balachandra Rao & HR Anuradha-Universities Press.
3. Differential Equations -Srinivas Vangala &Madhu Rajesh, published by Spectrum University Press.

\*\*      \*\*      \*\*